fra/52

# NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

**TECHNICAL NOTE 2742** 

BOUNDARY-LAYER DEVELOPMENT AND SKIN FRICTION

AT MACH NUMBER 3.05

By Paul F. Brinich and Nick S. Diaconis

Lewis Flight Propulsion Laboratory Cleveland, Ohio

Reproduced From Best Available Copy Washington

July 1952

20000508 216

MOO-08-2227

### NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

### TECHNICAL NOTE 2742

BOUNDARY-LAYER DEVELOPMENT AND SKIN FRICTION AT MACH NUMBER 3.05

By Paul F. Brinich and Nick S. Diaconis

### SUMMARY

Boundary-layer studies consisting of schlieren observations and momentum surveys were made on hollow cylinder models with their axes alined parallel to the stream. Results were obtained for three model diameters and for natural and artificially induced turbulent boundary-layer flows.

Transition Reynolds numbers were found to decrease with decreases in leading-edge thickness and with reductions in tunnel pressure level. Turbulent temperature-recovery factors generally decreased with increasing Reynolds number and were a maximum for the smallest transition Reynolds numbers.

The results of this investigation appeared to be consistent with the theoretical turbulent friction formulas of Wilson and with the extended Frankl-Voishel analysis of Rubesin, Maydew, and Varga. Velocity profiles in the outer portion of the boundary layer could be approximated reasonably with a 1/7 power profile and were found to be approximately similar in this region. Velocity profiles given by the Karman universal turbulent boundary-layer profile parameters were found to be similar in the laminar sublayer and in the turbulent region.

### INTRODUCTION

Total-pressure surveys of the turbulent boundary layer at supersonic speeds are made and analyzed in references 1, 2, and 3 for the purpose of determining skin-friction coefficients as a function of Reynolds number. Results of an investigation of a flat plate model spanning the tunnel are reported in reference 1. Turbulent boundary layers were formed by the natural transition from laminar to turbulent flow and surveys were made at several positions along the model length. The Mach number of the stream was varied from 1.70 to 2.19 and the tunnel was operated at a constant stagnation pressure at each Mach number, giving a maximum Reynolds number of about  $22 \times 10^6$  for the turbulent boundary layer. To obtain the results given in reference 3, a smaller flat plate model was used and turbulent boundary layers were formed by the rapid

245]

artificial transition to turbulent flow. A maximum Reynolds number of  $1.1\times10^6$  was attained. The stream Mach number was 2.5 and the stagnation pressures were 30 and 40 pounds per square inch absolute.

Integrated friction coefficients were obtained in reference 1 by equating the measured momentum defects to the drag and making suitable corrections to the length of turbulent run because of the presence of the laminar boundary layer upstream. In reference 3 corrections to the length of run were necessary because of the high initial thickness of the boundary layer near the leading edge caused by the coating used to promote early transition to turbulent flow.

The present investigation, which was made at the NACA Lewis laboratory, is an extension of the aforementioned experimental investigations to a higher Mach number and contains a more detailed investigation of the effect of Reynolds number variation on the boundary-layer development and skin-friction coefficient. The conventional flat plates of references 1 and 3 were replaced by hollow cylinders with axes alined parallel to the stream direction. It was believed that the flow over the cylinders would be less subject to disturbing influences caused by the thick tunnel side-wall boundary layers than the conventional flat test plate mounted from the two tunnel side walls. In order to determine whether the boundary layer developed in the same manner as on a flat plate, boundary-layer measurements were made on three cylinders having different diameters.

Tests were conducted at a stream Mach number of about 3.05 and at stagnation pressures from 7 to 50 pounds per square inch absolute. This range of pressure permitted a Reynolds number variation from about 1 to  $8\times10^6$  per foot, or a maximum Reynolds number of  $14\times10^6$ .

Each of the three models was tested with natural and artificial transition to turbulent boundary-layer flow to determine in what respect the two types of development are similar and whether it is possible to obtain a correlation of turbulent skin-friction coefficients from artifically turbulent boundary layers.

The analysis of the experimental results is made in a manner similar to that indicated in references 1 and 3 and, in addition, includes the measurement of the local skin-friction coefficient and a determination of the shape of the boundary-layer profile in terms of the Karman similarity parameters for turbulent boundary-layer flow.

### APPARATUS

The three basic cylinder models used in this investigation are shown in figure 1 together with pertinent dimensions. The addition of

NACA TN 2742

roughness near the leading edge on each of these models gave a total of six configurations tested. The models were 3, 4, and 5 inches in outside diameter and 31 inches in length. The steel models were turned, ground, and polished, and the leading edges were hardened to maintain their sharpness. A single strut was provided for mounting the cylinders on the tunnel side wall. Figure 2 shows a sketch of the 5-inch model in the tunnel and the instrumentation setup for surveying the boundary layer. The tunnel used for testing the model was the 1- by 1-foot variable Reynolds number tunnel, which is a nonreturn type having a stagnation pressure range of 5 to 52 pounds per square inch absolute.

Static-pressure orifices were provided along four lines on the top, bottom, and two sides of the models. Spacing between orifices was 3 inches on the probing side, and 6 inches on the top, bottom, and opposite side. Additional instrumentation was provided outside and inside the lip in some cases. Four insulated thermocouples were imbedded in the outside surface of the 5-inch cylinder just below the line of static-pressure orifices on the survey side of the model at distances of 3,  $6\frac{1}{2}$ ,  $12\frac{1}{2}$ , and  $18\frac{1}{2}$  inches from the leading edge.

The roughness used to cause early transition from laminar to turbulent flow consisted of a single layer of number 60 carborundum grit applied in a clear lacquer coating in the form of a band extending from the leading edge to 1/2 inch downstream. The coating had a decreased density near the leading edge to minimize its effective bluntness.

The conventional boundary-layer-type total-pressure probes used were made of 0.030- by 0.002-inch stainless-steel tubing flattened at the end to 0.006-inch thickness with a 0.002-inch-high opening. These probes are shown in figure 3. Probe (a) was used on the survey side of the model and was 3 inches long from tip to heel; probes (b) and (c) were used on the top and bottom of the model and were 4 inches long. Probe (a) was translated by a mechanism which had a to.0005-inch positioning accuracy. The average positioning accuracy relative to the model was about to.002 inch. Probes (b) and (c) were rotated by a mechanism having a comparable positioning accuracy. Total pressures were measured on mercury manometers and static pressures, on differential butyl phthalate manometers.

### PROCEDURE

Before making boundary-layer measurements on the three models, adjustments in angle of yaw and attack were made to minimize the differences of static pressure on opposite sides of the model. In each case the final adjustment of the model, which amounted to yawing it a maximum of  $1/2^{\circ}$  from the tunnel center line, yielded a pressure distribution in which opposite orifices had maximum pressure differences of about 3 percent. After proper alinement of the model had been achieved, static-pressure distributions were obtained at stagnation pressures of 7, 12, 20, 30, 40, and 50 pounds per square inch absolute for each of the three

models. Likewise, schlieren photographs were obtained to show the leading-edge shock formation and the boundary-layer development. For the 5-inch model, surface temperature measurements were made throughout the pressure range. The stagnation temperature was approximately constant at 50° F with a mean variation of 5° F and the dew point was kept below -40° F.

Total-pressure boundary-layer surveys were made at eight positions along the model 3 inches apart, starting 0.5 inch from the leading edge and extending 21.5 inches back. The stagnation pressures at which these surveys were made are indicated for each of the models in the following table:

Model diameter (in.)	Tunnel stagnation pressure (lb/sq in. abs)				
	Natural transition Artificial transition				
3	12, 50 12, 50				
4	12, 50				
5	7, 12, 20, 30, 50 7, 12, 20, 30, 50				

Additional check measurements on the top and bottom of the model were obtained to find whether the boundary-layer development about the model was symmetrical. All surveys were made after the model surface temperatures and pressures had reached equilibrium.

### Reduction of Pressure Survey Data

The first step in computing the various boundary-layer quantities used in the following analysis was to obtain the boundary-layer Mach number distributions using the total-pressure surveys and model surface static pressures. This was done by making the conventional assumption of a constant static pressure within the boundary layer normal to the surface and using the Rayleigh relation for a supersonic pitot tube. Because the external and internal flow Mach numbers did not differ greatly, it could be inferred that the flow over the cylinder is adiabatic and that the assumption of constant total temperature throughout the boundary layer is reasonable. With this assumption, velocity profiles were computed from the Mach number profiles using the expression

$$\frac{u}{u_1} = \frac{M}{M_1} \sqrt{\frac{1 + \frac{\Upsilon - 1}{2} M_1^2}{1 + \frac{\Upsilon - 1}{2} M^2}}$$

(All symbols used in this report are listed in the appendix.) Two-dimensional boundary-layer displacement thicknesses  $\delta^*$  were computed by the equation

245]

and the corresponding momentum thickness  $\theta$ , by

$$\theta = \int_0^{\delta} \frac{\rho u}{\rho_1 u_1} \left( 1 - \frac{u}{u_1} \right) dy$$

where

$$\frac{\rho}{\rho_1} = \frac{1 + \frac{\gamma - 1}{2} \, M^2}{1 + \frac{\gamma - 1}{2} \, M_1^2}$$

A more precise calculation of the momentum thickness, taking into account the cylindrical form of the model, was made using the equation (reference 4)

$$\Theta = \theta + \frac{1}{r} \int_{0}^{\delta} \frac{\rho u}{\rho_{1} u_{1}} \left(1 - \frac{u}{u_{1}}\right) y \, dy$$

where r is the radius of the cylinder. The contribution of the second term on the right side was a maximum of 14 percent for positions farthest downstream.

Although heat-transfer effects were assumed negligible, there still remains a question concerning the error resulting from assuming the total-temperature distribution in the boundary layer to be a constant. It is shown in reference 1 that this assumption has very little effect on the velocity or on the displacement and momentum thicknesses of turbulent profiles at Mach number 2. To check the validity of this assumption at a Mach number of 3.05, temperature distribution calculations based on the theory of reference 5 were made for four typical turbulent profiles using actual velocity profiles and observed wall temperature data. The maximum change in velocity from that obtained for the case of constant total temperature was  $+2\frac{1}{2}$  percent, and the average changes in displacement and momentum thicknesses were -0.3 and -2 percent, respectively.

In general, both the skin-friction coefficient and the Reynolds number used in an experimental correlation of the same must be based on some value of the dynamic pressure which is representative of the freestream value. Such values of the dynamic pressure were obtained from an

NACA IN 2742

arithmetic average of the free-stream Mach number along the cylinder. Because the friction coefficients (which also depend on the momentum thicknesses) were calculated assuming a zero pressure gradient, the observed momentum thickness had to be corrected for small deviations in Mach number from the arithmetic average obtained along the model. The method for making such corrections is given in reference 1 and was applied to the measured velocity profiles to obtain corrected values of momentum thickness. The maximum correction of the momentum thickness did not exceed 2 percent. All the values of momentum thickness, friction coefficient, and Reynolds number shown in the figures were corrected according to the preceding scheme.

### Accuracy of Pressure Measurements

Total-pressure measurements in the boundary layer were estimated to be accurate to ±0.03 inch of mercury and static pressures, to ±0.05 inch of butyl phthalate. These limitations resulted in average Mach number errors of ±0.03 for the lowest tunnel pressure level tests; higher pressures, of course, resulted in greater accuracy.

In computing the velocity profiles, the effective center of the pitot tube was taken as its geometric center, and the edge of the boundary layer was selected as the point where the velocity equaled about 99.9 percent of the free-stream velocity. Probable errors in computing momentum thickness based on the given accuracy in Mach number and the inherent accuracy of the probe positioning device were approximately ±1.5 percent.

The determination of the slope  $d\Theta/dx$  which was used to find the local friction coefficient was subject to large uncertainties because of the great latitude within which a fairing of the experimental points could be drawn. The probable error due to this fairing was estimated at  $\pm 10$  percent.

## RESULTS AND DISCUSSION

A CAN CONTRACTOR WITH THE STATE OF THE STATE

The ultimate purpose of this investigation is to correlate the skin-friction coefficients obtained from momentum surveys with the Reynolds number. Before this correlation can be made, however, several factors must be considered to determine whether the conditions of the experiment sufficiently approximate the assumptions of the theories with which the experimental results are to be compared. These factors are: the degree to which the actual pressure or Mach number gradient along the model approximates the zero gradient, the determination of the laminar and turbulent flow regions, the effect of the leading edge on the initial boundary-layer development, the consistency of the measured wall temperature-recovery factor with the assumption of zero heat transfer, and the effect of cylinder diameter on the boundary-layer development.

451

### Longitudinal Mach Number and Pressure Distributions

The longitudinal Mach number distributions for the 3-, 4-, and 5-inch models with natural and artificial transition are shown in figures 4(a), (b), and (c), respectively, at the various stagnation pressures. Mach numbers were obtained from probe total-pressure and model static-pressure data; most of the measurements were made along the side of the model.

The Mach number along the model generally increases from slightly downstream of the leading edge to x=15.5 inches; thereafter it drops to lower values farther downstream. According to the momentum equation, these changes in Mach number would cause errors in the value of the local friction coefficient computed on the basis of a zero Mach number gradient. These gradients introduce maximum errors of about 2 percent for x less than 15.5 inches and 10 percent for x greater than 15.5 inches on the 5-inch model having artificial transition, which represents the worst case.

A comparison of points on the top, bottom, and side of the model at equal distances from the leading edge reveals slightly higher Mach numbers and hence lower static pressures on the top and bottom of the model than on the side. Schlieren observation showed no stream disturbances, such as shock waves, which would cause such consistent variations in observed pressure. The existence of such disturbances is not precluded, however, since schlieren observations along a vertical light path, that is, through the top and bottom of the tunnel, were impossible. It is believed that the resulting pressure gradients around the body may cause secondary flows which would transport low energy air to the top and bottom of the model, giving more pronounced boundary-layer developments there.

### Schlieren Observations

Typical schlieren photographs of the flow past the 5-inch model at a stagnation pressure of 50 pounds per square inch absolute are shown in figure 5(a) for natural transition and in figure 5(b) for artificial transition. No tunnel stream shock waves are visible, indicating uniform flow in vertical planes parallel to the flow. The starting shock of the cylinder appears to be completely swallowed as indicated by the thin, almost straight, attached leading-edge shock. (Additional static-pressure instrumentation on the model interior indicated an internal Mach number of 2.8.) Hundreds of 6-microsecond duration flash schlieren photographs were taken, none of which showed evidence of high frequency intermittent spillage or shock oscillation at the leading edge.

The leading-edge shock for the artificial transition is stronger and steeper than for the natural transition, and is followed by an expansion region at the end of the leading-edge roughness. A second shock follows this region. The reflection location of the leading-edge

shock from the tunnel wall back to the model depends primarily on the model diameter. The distances from the leading edge where the reflected shock intersected the model are listed in the following table (no schlieren data were available for the 3- and 4-in. models with artificial transition):

Mod	Distance from leading edge		
Natural transition	Artificial transition	x (in.)	
5-in. 4-in. 3-in.	5-in.	19.2 22.1 24.6 18.3	

A comparison of the longitudinal Mach number distributions of figures 4(a), (b), and (c) and the respective distances in the preceding table shows that only the 5-inch model experiences significant effects on Mach number distribution due to the reflected leading-edge shock.

Data previously taken at the Lewis laboratory have shown that the transition from laminar to turbulent flow observed by the schlieren method can be correlated with the transition point obtained with pitot surveys. The schlieren method has been used in the present investigation, and figure 5(a) is a typical example of the appearance of the transition region. The position of the transition point varied with time; this fluctuation was observed by taking a large number of flash schlieren photographs. The extreme fluctuations of position were about 1 inch upstream and downstream of a given mean position. In figure 5(a) the transition locations on the top and bottom were about equal, but in some cases considerable differences in location were observed. An investigation was also made to determine whether there was any hysteresis lag in the position of the transition point, particularly in going from one pressure level to another. None was detected.

A plot of the transition Reynolds number based on the mean location of the transition point is given as a function of the leading-edge thickness for each of the various stagnation pressures in figure 6. The transition location is the average of the mean locations on the top and the bottom of the model as obtained from schlieren photographs. The model diameters corresponding to the four leading-edge thicknesses are indicated.

Two sets of data appear for the 4-inch model, corresponding to two thicknesses of the leading edge. In the beginning of the test program it was suspected that the sharpness of the leading edge may be an important factor in determining the boundary-layer development, since unusually

2451

A very large dependence of the transition Reynolds number on the tunnel stagnation pressure is indicated in figure 6. Changes in stagnation pressure from 7 to 40 pounds per square inch absolute yielded 2.2 increases in transition Reynolds number for each leading-edge thickness. The maximum total change in transition Reynolds number obtained by varying both leading-edge thickness and stagnation pressure is from 1.0 to 3.5×10<sup>6</sup>. Presumably still larger values could be obtained by increasing the leading-edge thickness above 0.012 inch.

The decreased transition Reynolds numbers observed at the low stagnation pressures are believed to be caused by the increased throttling in the air supply to the tunnel plenum chamber required to attain the lower stagnation pressures. Measurements of the instantaneous pressures in the plenum chamber with a Statham pressure transducer indicated that the maximum fluctuations in pressure were approximately equal at all stagnation pressures. Hence, the turbulence level, expressed as the ratio of pressure fluctuation to total pressure, increased for decreases in tunnel stagnation pressure. The magnitude of the maximum fluctuation was about 0.8 inch of mercury.

### Temperature-Recovery Factor

Temperature-recovery factors were computed from measurements of the wall temperature on the 5-inch model having natural and artificial transition in order to check the validity of the assumption of zero heat transfer made in the calculation of the experimental velocity and density distributions. These recovery factors are defined by

$$R = \frac{T_{W} - T_{\underline{1}}}{T_{O} - T_{\underline{1}}}$$

and are shown plotted against Reynolds number in figure 7 for the full range of stagnation pressure.

2451

An examination of the recovery factors obtained for the case of natural transition shows an intial increase up to the transition point  $({\rm Re_{x_T}}=1.0\times 10^6~{\rm to}~2.3\times 10^6~{\rm from~fig.~6})$  and a gradual decrease thereafter in the turbulent region. This trend agrees with the experimental results of reference 6 to within 1 percent on the recovery factor, but the results of reference 7 are about 6 percent higher. The spread in the values of the recovery factor in the region  $1\times 10^6 < {\rm Re_x} < 3\times 10^6$  appears to be related to the different transition Reynolds numbers observed at the various pressures in figure 6. Thus the high recovery factors noted for the runs with 7, 12, and 20 pounds per square inch absolute stagnation pressure are associated with the relatively early transition to turbulent flow. The runs with 30 and 50 pounds per square inch pressure, which had higher transition Reynolds numbers, had notably lower recovery factors.

All the artificial transition recovery factors shown in figure 7 are for turbulent boundary layers. At Reynolds numbers from 2 to  $12 \times 10^6$  these recovery factors agree fairly well with those obtained for natural transition flows. Below a Reynolds number of  $2 \times 10^6$  they continue to increase above the values attained at the high Reynolds numbers and above the values shown for the laminar boundary-layer flow. Similar observations were made in reference 5 for the flow over a flat plate at a Mach number of 2.4.

The theoretical turbulent recovery factors of reference 5 for a Mach number of 3.05 are about 4 percent lower than the results obtained in this investigation.

### Effect of Model Diameter and Leading-Edge

### Thickness on Boundary-Layer Development

Measurements were made on three models of different diameters to determine the variation of boundary-layer development with surface curvature transverse to the flow. It was hoped that the trends observed for the various diameter models could be extrapolated to establish a relation for the boundary-layer development on a flat plate. However, the very great dependence of the boundary-layer development on the thickness of the leading edge, which varied from one model to another, precluded even a qualitative estimate of the effect of model diameter on the boundary-layer development.

Figures 8(a) and 8(b) show the variation of momentum thickness as a function of the leading-edge thickness for stagnation pressures of 12 and 50 pounds per square inch absolute and natural transition. Near the leading edges where the flows are predominately laminar the momentum thicknesses are largest for the 0.006-inch and least for the 0.003- and 0.002-inch leading edges. Farther downstream in the turbulent region

the reverse trend is apparent. A comparison of the momentum thicknesses at x=21.5 inches for the various leading edges shows that reductions in momentum thickness of 10 to 20 percent are possible by blunting the leading edge from 0.002 to 0.006 inch. Presumably larger reductions in drag would be indicated by data from the 4-inch model having the 0.012-inch leading edge if such data were available.

The artificial transition results of figure 8(c) were obtained for turbulent boundary layers and indicate decreasing momentum thicknesses for thicker leading edges. Although the trends for the artificial transition data followed those for the natural transition in the turbulent region, the distributions of momentum thickness along the model were very irregular.

Because it is impossible to establish a relation between the cylinder and flat-plate boundary-layer developments from the experimental results, some alternate approach must be employed to justify the comparisons to be made between cylinder and flat-plate turbulent friction coefficients. If the relation between the turbulent friction coefficients for a cylinder and a flat plate may be assumed approximately similar to the relation between the laminar friction coefficients, then such a comparison may be justifiable. Theoretical calculations of the incompressible laminar friction coefficients made for the 3-inch cylinder model using the analysis of reference 8 show a maximum increase of 2 percent over those for a flat plate at a stagnation pressure of 12 pounds per square inch absolute, indicating that the comparisons to be made herein are probably valid.

Comparison of Experimental and Theoretical Laminar Velocity Profiles

Laminar-type velocity profiles were observed on all the models having natural transition at Reynolds numbers less than the transitional values indicated on figure 6, and on the 5-inch model having artificial transition at a stagnation pressure of 7 pounds per square inch absolute for the positions 0.5, 3.5, and 6.5 inches from the leading edge. Figure 9 shows the experimental laminar profiles obtained with natural transition on the side of the 5-inch model with the 0.003-inch leading-edge thickness and on the 4-inch model with the 0.012-inch leading-edge thickness. The theoretical dimensionless velocity and distance parameters of reference 9 have been used to present the experimental data, and the theoretical curve for M = 3.05 has been included for comparison.

The first observation to be made in figure 9 is that almost all the experimental points fall to the right of the theoretical line, indicating a more rapid boundary-layer development than that predicted by theory. That this greater initial growth is dependent on the thickness of the leading edge can be seen by comparing the two profiles obtained on the 4-inch model with the 0.012-inch leading edge at the 0.5-inch position with those obtained on the 5-inch model having a 0.003-inch leading edge.

2451

This comparison of two different diameter models is justified because the 5-inch model had the same boundary-layer profile near the leading edge as the 4-inch model with the 0.002-inch leading edge. The 0.012-inch leading edge gives boundary layers far thicker than the 0.003-inch edge. In addition, the boundary layers with the 0.003-inch edge have an inflection in the profile near the free-stream edge of the boundary layer which gives boundary-layer velocities in excess of stream velocities by as much as 3 percent. From the results concerning transition discussed earlier, the generalization may be made that the thicker leading edge gives thicker initial boundary layers and larger transition Reynolds numbers than the thin leading edge. Further, the appearance of the velocities in excess of the free-stream value in the profile is associated with a decrease in the transition Reynolds number. This latter point was more firmly established for the 3-inch model in which the excess velocity in the profile was almost indiscernible and the transition Reynolds number was substantially higher than for the other models having larger excess velocities. The excess velocity regions shown in figure 9 are not particularly impressive when shown in terms of u/u but become very substantial in the indicated pitot pressure surveys. These regions were detected as far downstream as 3.5 inches; they diminish in intensity as distance increases.

A further comparison of experiment and theory in figure 9 shows that discrepancies diminish with increasing distance downstream and with decreasing total pressures. The diminution with distance is to be expected since the effect is associated with the leading edge. The thinnest leading edges gave the best agreement with theory.

A possible reason for the poor agreement between the experimental measurements and theory in the region near the leading edge may be that the large probe size relative to the boundary-layer thickness made it impossible to obtain accurate, undisturbed boundary-layer measurements. However, the changes in shape of the measured profiles corresponding to small changes in leading-edge thickness were associated with changes in transition location as noted in schlieren photographs. For this reason it must be concluded that the probes are sufficiently sensitive to detect qualitative changes in profile caused by independent variations, such as changes in the leading-edge thickness.

Another possible source of error arose from vibrations of the models, which were strongest over the forward portion and at high stagnation pressures. These vibrations resulted from the long cantilever mounting from the single support strut at the rear and may contribute slightly to the measured boundary-layer thickness over the forward portion of the model. The turbulent profiles are not believed to be noticeably affected by this vibration.

Two methods for studying similarity among turbulent velocity profiles are in common usage. In the first method the various turbulent velocity profiles are expressed in terms of the nondimensional velocity u/u<sub>1</sub> distance  $y/\delta$  or  $y/\Theta$ . This method has been used in the analysis of incompressible and compressible flow boundary layers and is usually considered to apply only to the outer part of the turbulent boundary layer. In the second method the similarity parameters are the nondimensional friction velocity ratio  $u/\sqrt{\tau_0/\rho}$  and the friction distance parameter  $(\rho \sqrt{\tau_0/\rho})(y/\mu)$ . These parameters define the Kármán universal turbulent logarithmic velocity profile which follows from the turbulent mixing length theory. This method has been used extensively for the analysis of subsonic turbulent boundary-layer data, both incompressible and compressible (e.g., references 10 and 11); however, its application to supersonic turbulent boundary-layer data is almost unknown. Both these methods will be used to analyze the boundary layers measured in this investigation and to determine their range of application.

The subject of greatest practical interest here, however, is the determination of the friction coefficient over the widest possible range of Reynolds number. Two procedures for presenting skin friction data are commonly used. The first procedure relates the integrated flat-plate friction coefficient  $\mathcal{C}_{\mathbf{f}}$  to the Reynolds number based on length of run  $\mathrm{Re}_{\mathbf{x}}$  where  $\mathcal{C}_{\mathbf{f}}$  is determined from

$$C_f = \frac{20}{x}$$

This method will be used to present friction coefficient results for both natural and artificial transition boundary layers. Since for the case of natural transition a part of the measured momentum thickness  $\Theta$  and the length of run x or both may be thought of as due to the upstream laminar layer, the turbulent friction coefficient  $C_f$  as defined will be incorrect and result in low values of the coefficient. Hence, a correction equivalent to increasing the momentum thickness  $\Theta$  or decreasing the length of run x or both is necessary to obtain a friction coefficient for comparison with empirical formulas for turbulent two-dimensional flow. Such corrections can be made with low-speed empirical friction laws as guides.

In the second procedure the local friction coefficient  $c_{\mathbf{f}}$  is related to the Reynolds number based on momentum thickness  $\text{Re}_{\Theta}$ . This method requires no correction to the momentum thickness or length of run since the relation between  $c_{\mathbf{f}}$  and  $\text{Re}_{\Theta}$  is generally believed to be fairly independent of the previous history of the boundary layer and the location

of the transition point. The validity of the two methods will then be investigated by comparing the results obtained from each.

Turbulent velocity profiles  $u/u_1$  versus  $y/\Theta$ . - Turbulent velocity profiles  $u/u_1$  against  $y/\Theta$  are plotted in figures 10(a) and 10(b) for representative locations and pressures along the side of the 5-inch model for both natural and artificial transition. These plots show approximate similarity of the turbulent profiles whether produced naturally or artificially for values of  $y/\Theta > 3.0$  and, when compared with the power profiles indicated by the solid lines, show the closest agreement with the 1/7 power law. The somewhat higher degree of similarity in the artificial transition plots for the region near the wall reflects the smaller variation in  $\Theta$  along the model length compared with that for the natural transition.

Integrated friction coefficients. - In order to simplify the presentation of the integrated friction coefficient data and to facilitate the subsequent corrections to the momentum thickness and length of run necessary to obtain coefficients for 100 percent turbulent flow, the friction coefficient  $\mathbf{C}_{\mathbf{f}}$  has been expressed in terms of the Reynolds numbers based on the momentum thickness and length of run

$$C_{f} = \frac{2\Theta}{x} = \frac{2 \text{ Re}_{\Theta}}{\text{Re}_{x}}$$

If it is assumed that the integrated friction coefficient can be expressed in terms of the Reynolds number raised to a power as for incompressible completely turbulent flow

$$C_{\mathbf{f}} = \frac{K}{Re_{\mathbf{x}}^{n}}$$

where K and n are constants, then substituting the former expression for  $\mathbf{C}_{\mathbf{f}}$  gives the following:

$$Re_{\Theta} = \frac{K}{2} (Re_{x})^{1-n}$$

A plot of these variables  $\text{Re}_\Theta$  and  $\text{Re}_{\mathbf{X}}$  on log-log coordinates yields a straight line, the slope of which is l-n.

All measurements of  ${\rm Re}_\Theta$  and  ${\rm Re}_{\rm X}$  for natural and artificial transition on all models are plotted in figures ll(a) and ll(b). A single line approximating the average distribution of the experimental

2451

points has been faired in figure ll(a). This line is a curve concave downward. If the requirement for purely turbulent flow that this line be straight is to be satisfied, then a constant addition  $\Delta \text{Re}_{\Theta} = 0.6 \times 10^3$  or a subtraction  $\Delta \text{Re}_{X} = 0.6 \times 10^6$  or some combination of the two must be made. Accordingly, such corrections to the original curve have been made and are represented by the single dot-dash straight line of figure ll(a). Because the final curve has a slope so nearly equal to 1, a correction involving  $\Delta \text{Re}_{\Theta}$  gives the same corrected line as a correction involving  $\Delta \text{Re}_{\Theta}$ .

The corrected line may be represented by an equation given in terms of the integrated friction coefficient

$$C_f = \frac{0.039}{Re_x^{0.19}}$$

or if a compressibility factor of the form  $\left(1 + \frac{\gamma - 1}{2} M_1^2\right)^m$  is separated out and the constant 0.074 of the incompressible law is assumed correct,

$$C_f = \frac{0.074}{\text{Re}_x^{0.19}} \left(1 + \frac{\gamma - 1}{2} M_1^2\right)^{-0.6}$$

The friction coefficient formulas of von Karman (reference 12), of Wilson (reference 2), and of Rubesin, Maydew, and Varga in their extended Frankl and Voishel analysis (reference 3) are shown in figure 11(a) all based on the same linear temperature-viscosity relation. The formulas given by references 2 and 3 are seen to best fit the corrected experimental data.

Strictly speaking, the method of applying these corrections is not exact because the subtraction or addition of a constant amount  $\Delta Re_{\rm X}$  or  $\Delta Re_{\rm O}$ , respectively, implies that the turbulent flow begins at the same Reynolds number regardless of stagnation pressure or leading-edge thickness. Figure 6 showed that, actually, the transition Reynolds number varied over a wide range which was substantially higher than the value of  $\Delta Re_{\rm X} = 0.6 \times 10^6$  used for one of the two possible corrections in figure ll(a). However, there is no reason why the apparent beginning of the turbulent boundary layer ( $\Delta Re_{\rm X} = 0.6 \times 10^6$ ) should correspond to the actual beginning of it, for the former will have its origin in the transitional layer immediately following the initial laminar layer.

Nevertheless, attempts were made to correct each set of data individually so as to separate out the effects of a varying transition Reynolds number. Because of extraneous effects, for example, possibly

those associated with the leading edge or secondary flows, some of the individual sets of data exhibited some serious inconsistencies, such as transition Reynolds numbers  $\mathrm{Re}_{\mathrm{X}_{\mathrm{T}}}$  having negative values. Rather than an attempt to rationalize these inconsistencies or to discard the irregular data points, the procedure of including all the points in one plot of  $\mathrm{Re}_{\mathrm{\Theta}}$  against  $\mathrm{Re}_{\mathrm{X}}$  was decided upon. The results obtained by this method should then be understood to contain an average of all the results corresponding to some average transition Reynolds number.

The corresponding results for the models having artificial transition are shown in figure 11(b), and it is to be noted that the experimental points can no longer be approximated by a single curved line, but rather are approximated by a family of curves - one for each pressure. The dot-dash line shown is taken directly from figure 11(a) where it represented the final correction of the original experimental results. In figure 11(b) the experimental points fall to the left of the corrected line, necessitating the opposite corrections, that is, a subtraction  $\Delta \text{Re}_{0}$  or addition  $\Delta \text{Re}_{x}$ . This time, however, a specific correction varying with the pressure is required for the uncorrected experimental curves to approximate the dashed line. Approximate corrections  $\Delta \text{Re}_{0}$  and  $\Delta \text{Re}_{x}$  are listed in the following table for the artificial turbulence flow on all three models:

	_				50
$P_{\Omega}$	7	12	20	30	50
(13 /- a in sha)					
(1b/sq in. abs)				7	3
∆Re⊜	0	$-0.4 \times 10^3$	-0.8×10 <sup>5</sup>	-1.3×10 <sup>3</sup>	$-2.7 \times 10^3$
	1	.4×10 <sup>6</sup>	.8×10 <sup>6</sup>		3.5×10 <sup>6</sup>
$\Delta  exttt{Re}_{\mathbf{X}}$	0	.4×10°	.0710	1.56.10	0.0 20

Thus, very large corrections are indicated for the highest stagnation pressures and negligible ones, for the lowest. This increased discrepancy at high pressures appears to be analogous to the increased discrepancy between experiment and theory in the case of the laminar boundary layer (fig. 9) where the same behavior with pressure was noted. Likewise, the greatest percentage deviations in the artificial turbulent boundary-layer development expressed in terms of the momentum thickness occurred near the leading edge, again comparable with the laminar boundary-layer case where the poorest agreement between experiment and theory was observed closest to the leading edge. The effect of adding roughness at the leading edge is therefore to cause a disturbance which increases the initial momentum thickness and which increases with the pressure or density.

Local friction coefficients. - Because of the arbitrary nature of the assumptions used to correct the measured values of  ${\rm Re}_{\rm X}$  and  ${\rm Re}_{\rm O}$ 

The curves of momentum thickness against x which were faired through the experimental points are shown in figure 12. A careful examination of the experimental points shows that the momentum thickness on the top and the bottom of the model was almost always larger than on the side. For this reason the curves faired through the experimental points represent average values among the top, bottom, and side. These large differences in boundary-layer development predominate in the turbulent region and appear to be caused by differences in the location of the transition point or by generally low static pressures on the top and the bottom of the model. In the laminar region the development in the three circumferential positions is very nearly equal.

The values of  $d\Theta/dx$  and  $Re_\Theta$  obtained with the aid of the faired curves of figure 12 are shown plotted in figure 13. Also shown are the semiempirical curves of Wilson (reference 2), of Rubesin, Maydew, and Varga's extended Frankl and Voishel analysis (reference 3), and of von Karman (reference 12), and the laminar curve of Chapman and Rubesin (reference 9), all with a linear temperature-viscosity relation. A comparison in figure 13(a) of the experimental results and the theories of references 2 and 3 shows good agreement up to  $Re_\Theta = 5000$ . Above this value the experimental points show a general downward trend.

Figure 13(b) shows the local friction coefficient plot for artificial transition together with the theoretical turbulent curves indicated in figure 13(a). In this case there is little correlation between experiment and theory. The discrepancy in the slopes of the data is greatest at the high pressures and least at the low, which was a characteristic observed to a certain extent for the natural transition results and also earlier for the uncorrected plot of  $\text{Re}_\Theta$  against  $\text{Re}_{\text{X}}$  for artificial transition (fig. 11(b)).

In order to compare the friction coefficients obtained by the two methods for both the natural and artificial transition, the equations obtained from the results of figures ll(a) and ll(b) were converted to the d $\Theta$ /dx against Re $\Theta$  coordinate system of figure 13 and are presented with the local friction coefficients in figure 14. Very good agreement between the two methods is apparent for the natural transition up to Re $\Theta$  = 5000. The artificial transition results show little correlation throughout. These results show that fairly typical correlations of

turbulent friction coefficient with Reynolds number are possible without resort to correction of any kind for the case of natural transition boundary-layer flow. Such correlations are not possible for the case of artificially turbulent flows.

Turbulent velocity profiles u+ against y+. - The Kármán similarity parameters u+ and y+ are given by the following expressions; local values of density and viscosity and wall values for the shear stress are used:

$$u^{+} = \frac{u}{\sqrt{\frac{\tau_0}{\rho}}} = \frac{u}{u_1} \sqrt{\frac{\rho}{\rho_1}} \sqrt{\frac{2}{c_f}}$$

$$y^{+} = \frac{\rho y \sqrt{\frac{\tau_{0}}{\rho}}}{\mu} = \frac{u_{1}y}{\nu} \sqrt{\frac{\rho_{1}}{\rho}} \sqrt{\frac{c_{f}}{2}}$$

The assumptions of a constant total temperature and a linear temperature-viscosity relation were used in computing the quantities  $u^+$  and  $y^+$  by the following equations, which are related to the stagnation conditions and the Mach number:

$$u^{+} = \frac{M}{M_{1}} \sqrt{\frac{2}{c_{f}}}$$

$$y^{+} = \frac{\sqrt{\gamma RT_{0}}}{v_{0}} M_{1} \frac{\left(1 + \frac{\gamma - 1}{2} M^{2}\right)^{\frac{2 - \gamma}{\gamma - 1}}}{\left(1 + \frac{\gamma - 1}{2} M_{1}^{2}\right)^{\frac{\gamma}{\gamma - 1}}} y \sqrt{\frac{c_{f}}{2}}$$

In order to compute these parameters it is necessary to know the local coefficients  $c_{\mathbf{f}}$  for each profile. These were obtained from the experimental curves of figure 14. Each of the several determinations of friction coefficient shown in figure 14 was tried to find which gave similarity among the various profiles in the turbulent region nearest the wall; the curve obtained from the plot of Reg against  $\mathrm{Re}_{\mathbf{X}}$ , where corrections for the effective leading edge or momentum defect were made, gave the most satisfactory results for both the natural and artificial transition boundary layers. The curves obtained from the plot of  $c_{\mathbf{f}}/2$  against  $\mathrm{Re}_{\mathbf{G}}$  for the artificial transition (fig. 13(b)) gave friction coefficients which produced very large discrepancies among the various

Charles San Spirit

Even when the friction coefficient results based on the correction method of figures ll(a) and ll(b) were used, a slight deviation from similarity was observed. This deviation was corrected to a mean line representative of all the profiles measured by adjusting the friction coefficient a constant amount for each individual profile, ±5 percent on the average. The plots of u<sup>+</sup> against log y<sup>+</sup> obtained with these corrections to the friction coefficient are shown in figures 15(a) and 15(b) for the same turbulent profiles presented earlier in figures 10(a) and 10(b), respectively. Good similarity is apparent throughout the entire range of values of u<sup>+</sup> and log y<sup>+</sup> except near the outer edge of the boundary layer where the maximum value of u<sup>+</sup> is reached. The value of u<sup>+</sup> there is given by

$$u^+_{max} = \sqrt{\frac{2}{c_f}}$$

This value of u<sup>+</sup>max is probably not the true maximum value of u<sup>+</sup> at the edge of the boundary layer, because the shear stress there has been assumed equal to the wall value. Small reductions in the shear stress or friction coefficient near the edge of the boundary layer therefore could produce similarity throughout the entire boundary layer. The greater departure from similarity for the artificial transition boundary layer compared with the natural in the region near the stream edge is caused by increased mixing, which extends the velocity boundary layer into a region of relatively low shearing stress.

Included in figure 15 for comparison with the experimental results are the theoretical laminar sublayer and turbulent layer curves for incompressible flow from reference 10 and some theoretical turbulent layer curves for compressible flow computed from reference 11. Making due allowances for the rather poor accuracy in the laminar sublayer allows this portion of the experimental boundary layer to be easily distinguished and identified with the theoretical laminar sublayer curve.

The theoretical representation for incompressible turbulent flow is shown by the single straight line of reference 8. The equation of this line is

$$u^+ = 5.5 + \frac{1}{K} \log y^+$$

2451

where K = 0.40 and is universal for all incompressible turbulent boundary layers. The method used in reference 11 to determine the effect of compressibility resulted in an expression for the compressible turbulent region where u<sup>+</sup> is a function of both y<sup>+</sup> and the shear stress or friction coefficient. Hence, the theoretical compressible turbulent flow region will be represented by a family of lines depending on the value of the shear stress assumed. The compressible turbulent curves shown in figure 15 were computed by the method of reference 11 for a stream Mach number of 3.05 and two typical values of the local friction coefficient, 0.00144 and 0.00250. The constant K was taken as 0.40.

A comparison of the compressible flow theory with the experimental results shows that the general theoretical trends are approximately borne out by experiment. Somewhat better agreement between the two could be obtained by further adjustment of the theoretical constant K and of the integration constant in the expression of reference 11 for the compressible turbulent flow region.

When the effect of compressibility is considered as in reference ll, the theoretical profiles depend on the particular value of friction coefficient chosen. The effect of differences in the assumed friction coefficients is small near the wall and increases as the edge of the boundary layer is approached, producing a distinct profile for each value of the friction coefficient. The experimental friction coefficients were modified so as to make the experimental profiles coincide in the region of  $\log y^+ = 1.7$ , and similarity throughout almost the entire boundary layer resulted. The agreement between experiment and theory in the region of  $\log y^+ = 1.7$  is found to be good, but as larger values of  $\log y^+$  are taken the agreement diminishes. The experimental points are seen to form a universal curve throughout the boundary layer which agrees with the theoretical curve only in the region near the wall. In the outer region where each of the theoretical curves depends on the value of the friction coefficient assumed, the agreement is poor.

Since small changes in the measured friction coefficient were necessary to establish the similarity of the turbulent velocity profiles, it is of interest to note what differences have been made in the curve of  $c_f/2$  against Re $_{\Theta}$  originally taken from figure 14. In figure 16 are shown the original curve and the corrected values of the friction coefficient necessary to establish similarity in figures 15(a) and 15(b). Both the natural and artificially turbulent boundary-layer results are shown and are seen to agree closely. The corrections to the original curve did not exceed 10 percent. It thus appears that if the profiles are made similar by adjustment of the local friction coefficients, then these friction coefficients remain continuous and smooth functions of Re $_{\Theta}$  as they were before adjustment and a good correlation is obtained both for natural and for artificial transition.

### SUMMARY OF RESULTS

The following results were obtained from the investigation of the boundary-layer development in a zero pressure gradient at Mach number 3.05:

- 1. The position of transition varied with time, the extreme positions being about 1 inch upstream and downstream of a mean location.
- 2. The transition Reynolds number was found to increase for increasing stagnation pressures and for increasing leading-edge thicknesses. The maximum variation in transition Reynolds number was from 1.0 to  $3.5 \times 10^6$ .
- 3. Turbulent temperature recovery factors were found to decrease slightly with increasing Reynolds number. The largest values of the recovery factor were found for the initially turbulent region and increased with decreasing transition Reynolds number. Natural and artificial transition flows gave equal recoveries in the turbulent region for equal Reynolds numbers.
- 4. No distinct model diameter effect was found in the boundarylayer growth. If such an effect existed, it was obscured by slight variations in the leading-edge thickness for the different models. The thickness of the leading edge had a pronounced effect on the boundarylayer development.
- 5. The agreement between the experimental and theoretical laminar boundary-layer profiles was excellent for low stagnation pressures, large distances downstream of the leading edge, and small leading-edge radii. Possible errors due to the relatively large size of the probe compared with the boundary-layer thickness may have some effect on the quantitative results found nearest the leading edge, but the general trends observed are probably correct.
- 6. Naturally and artificially turbulent boundary-layer profiles of the dimensionless velocity and distance parameters,  $u/u_1$  against  $y/\Theta$ , showed approximate similarity in the outer portion of the boundary layer, and the approximation to the power profile was best for a power profile exponent N equal to 7.
- 7. Integrated turbulent friction coefficients for natural and artificial transition were correlated against Reynolds number based on length of run by suitable corrections to account for transition and leading-edge effects. Good agreement with the theoretical friction coefficient formulas of Wilson and of Rubesin, Maydew, and Varga in their extended Frankl and Voishel analysis was obtained.

451

- 8. Local turbulent friction coefficients for natural and artificial transition were correlated against Reynolds number based on momentum thickness without making any corrections to account for transition and leading-edge effects. Good agreement with theory was obtained for the natural transition boundary layers up to a Reynolds number of 5000. Very poor agreement was found for the artificial transition boundary layers.
- 9. Naturally and artificially turbulent boundary-layer profiles expressed in terms of the Kármán turbulent profile velocity and distance parameters u<sup>+</sup> and log y<sup>+</sup>, respectively, showed similarity throughout the boundary layer except for the region nearest the stream edge. The departure from similarity was greatest for the artificial transition boundary layers and was probably caused by a more extended region of low shear turbulent mixing.

Lewis Flight Propulsion Laboratory
National Advisory Committee for Aeronautics
Cleveland, Ohio, April 10, 1952

2451

### APPENDIX - SYMBOLS

The following symbols are used in this report:

c proportionality constant in viscosity-temperature relation given in reference 9

 $c_f$  local friction coefficient,  $\tau_0/\rho_1 u_1^2/2$ 

 $c_f$  integrated friction coefficient, friction drag/ $\rho_1 u_1^2/2$ 

m exponent of compressibility factor

M Mach number

M<sub>1</sub> stream Mach number

N exponent in power profile relation,  $\frac{u}{u_1} = \left(\frac{y}{\delta}\right)^{\frac{1}{N}}$ 

n exponent of Reynolds number in friction formula

P<sub>O</sub> stagnation pressure

r radius of model

R temperature-recovery factor

 $\operatorname{Re}_{\mathbf{X}}$  Reynolds number based on length of run

Ree Reynolds number based on momentum thickness

 $\operatorname{Re}_{\mathbf{X}_{\operatorname{TP}}} \operatorname{Re}_{\mathbf{X}}$  of transition

T<sub>1</sub> stream static temperature

T<sub>O</sub> stream total temperature

 $\mathbf{T}_{\mathbf{W}}$  wall temperature

u velocity

u<sub>l</sub> stream velocity

u<sup>+</sup> Kármán turbulent boundary-layer velocity parameter

x distance along mode: from leading edge

y distance normal to model

y<sup>+</sup> Kármán turbulent boundary-layer distance parameter

- γ ratio of specific heat at constant pressure to specific heat at constant volume
- δ boundary-layer thickness
- δ\* two-dimensional displacement thickness
- $\theta$  two-dimensional momentum thickness
- three-dimensional momentum thickness on cylindrical body
- μ viscosity
- kinematic viscosity
- o density
- $\rho_1$  stream density
- τ<sub>O</sub> shear stress at wall

### REFERENCES

- Wilson, R. E., Young, E. C., and Thompson, M. J.: 2nd Interim Report on Experimentally Determined Turbulent Boundary Layer Characteristics at Supersonic Speeds. CM-501, DRL-196, Defense Res. Lab., Univ. Texas, Jan. 25, 1949. (Bur. Ord. Contract NOrd-9195.)
- 2. Wilson, R. E.: Turbulent Boundary Layer Characteristics at Supersonic Speeds Theory and Experiment. CM-569, DRL-221, Defense Res. Lab., Univ. Texas, Nov. 21, 1949. (Bur. Ord. Contract NOrd-9195.)
- 3. Rubesin, Morris W., Maydew, Randall C., and Varga, Stevan A.: An Analytical and Experimental Investigation of the Skin Friction of the Turbulent Boundary Layer on a Flat Plate at Supersonic Speeds. NACA TN 2305, 1951.
- 4. Tetervin, Neal: Approximate Formulas for the Computation of Turbulent Boundary-Layer Momentum Thicknesses in Compressible Flows. NACA ACR L6A22, 1946.
- 5. Tucker, Maurice, and Maslen, Stephen H.: Turbulent Boundary-Layer Temperature Recovery Factors in Two-Dimensional Supersonic Flow. NACA TN 2296, 1951.
- 6. Staldter, Jackson R., Rubesin, Morris W., and Tendeland, Thorval: A Determination of the Laminar-, Transitional-, and Turbulent-Boundary-Layer Temperature-Recovery Factors on a Flat Plate in Supersonic Flow. NACA TN 2077, 1950.

- 7. Eber, G. R.: Recent Investigation of Temperature Recovery and Heat Transmission on Cones and Cylinders in Axial Flow in the N.O.L. Aeroballistics Wind Tunnel. Jour. Aero. Sci., vol. 19, no. 1, Jan. 1952, pp. 1-6.
- 8. Seban, R. A., and Bond, R.: Skin-Friction and Heat-Transfer Characteristics of a Laminar Boundary Layer on a Cylinder in Axial Incompressible Flow. Jour. Aero. Sci., vol. 18, no. 10, Oct. 1951, pp. 671-675.
- 9. Chapman, Dean R., and Rubesin, Morris W.: Temperature and Velocity Profiles in the Compressible Laminar Boundary Layer with Arbitrary Distribution of Surface Temperature. Jour. Aero. Sci., vol. 16, no. 9, Sept. 1949, pp. 547-565.
- 10. von Kármán, Th.: Turbulence and Skin Friction. Jour. Aero. Sci., vol. 1, no. 1, Jan. 1934, pp. 1-20.
- ll. Deissler, Robert G.: Analytical and Experimental Investigation of Adiabatic Turbulent Flow in Smooth Tubes. NACA TN 2138, 1950.
- 12. de Kármán, Th.: The Problem of Resistance in Compressible Fluids.
  Quinto Convegno "Volta," Reale Accademia d'Italia (Roma), Sett. 30Ott. 6, 1935, pp. 3-57.

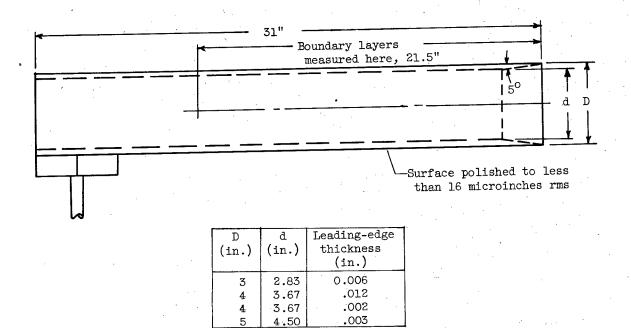


Figure 1. - Cylinder model dimensions.

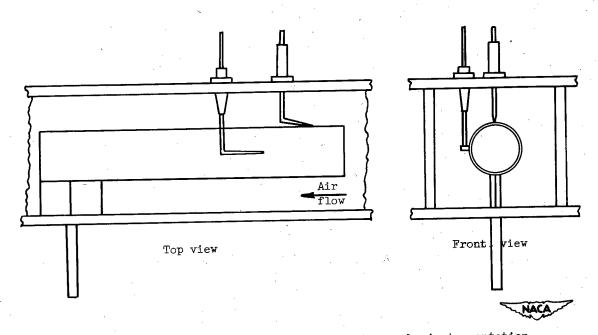
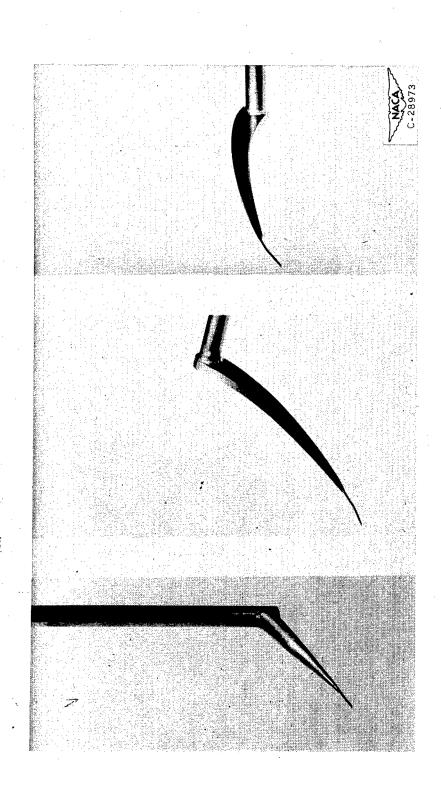


Figure 2. - Five-inch model in tunnel showing probe instrumentation.

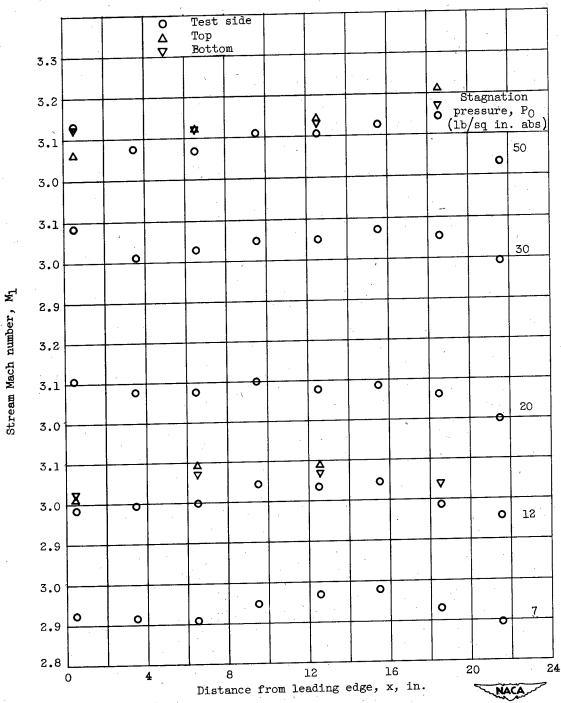


(b) Top probe.

(a) Side probe.

(c) Bottom probe.

Figure 3. - Total-pressure probes used for boundary-layer surveys.



(a) Natural transition, 5-inch model.

Figure 4. - Mach number distributions.

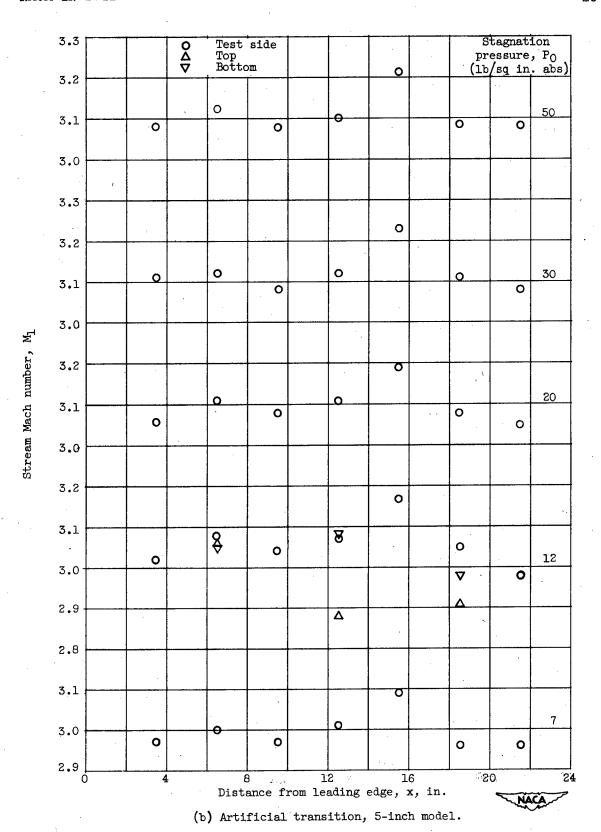
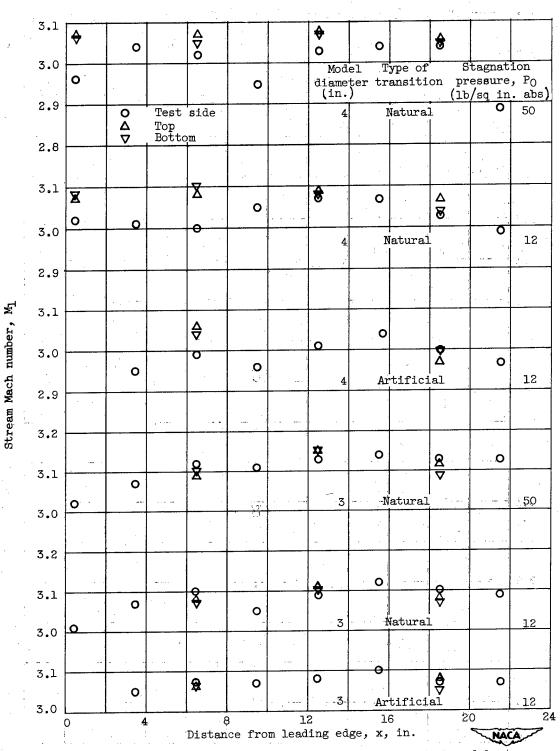
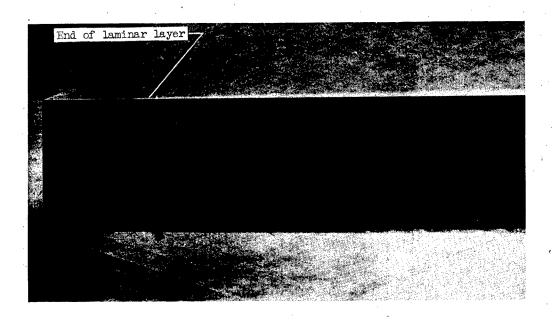


Figure 4. - Continued. Mach number distributions.

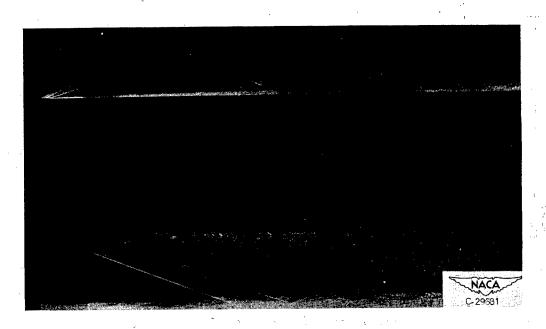


(c) Natural and artificial transition, 3- and 4-inch models.

Figure 4. - Concluded. Mach number distributions.

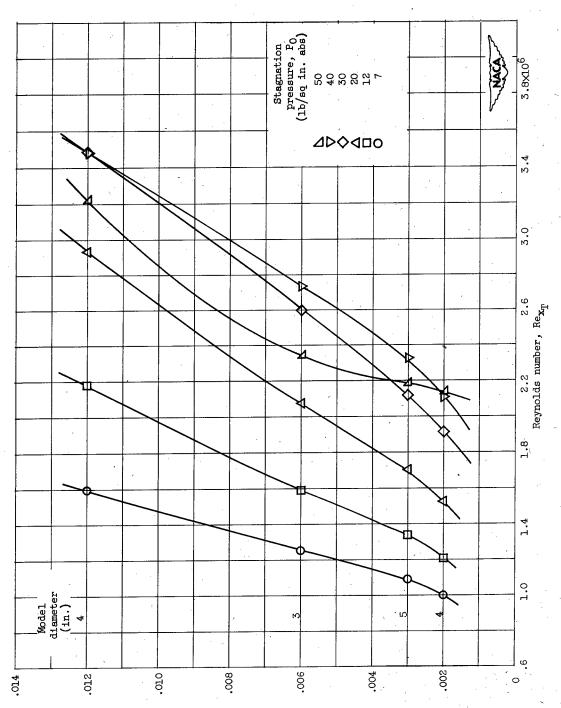


(a) Natural transition.



(b) Artificial transition. Stagnation pressure, 50 pounds per square inch absolute.

Figure 5. - Schlieren photograph of 5-inch model.



Leading-edge thickness, in.

Figure 6. - Variation of transition Reynolds number with leading-edge thickness for all models.

5T

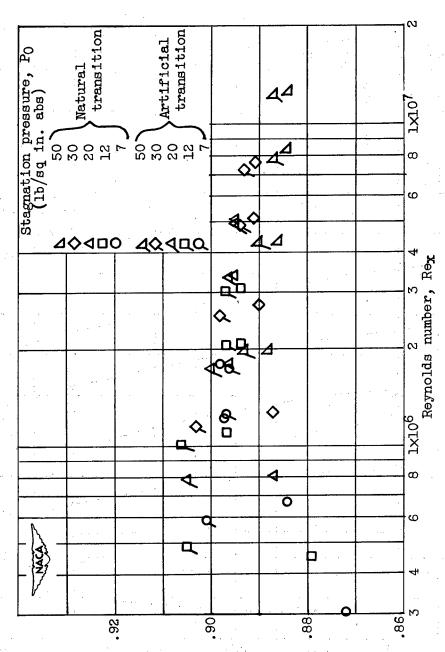
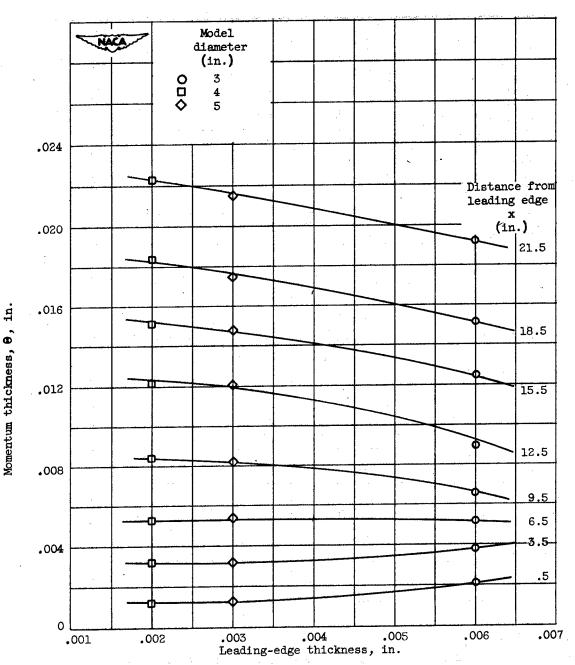
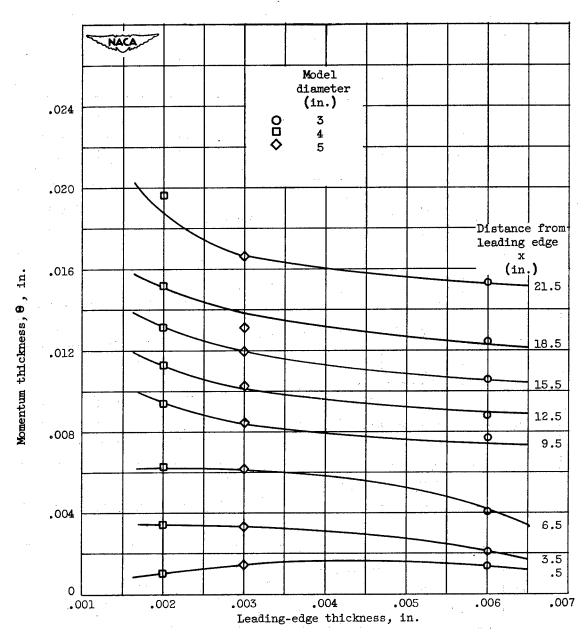


Figure 7. - Variation of recovery factor with Reynolds number



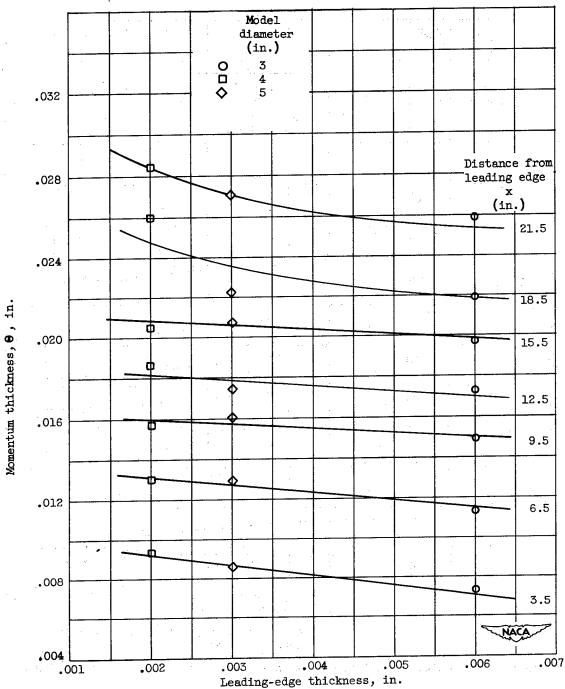
(a) Natural transition, stagnation pressure of 12 pounds per square inch absolute.

Figure 8. - Effect of leading-edge thickness on momentum thickness.



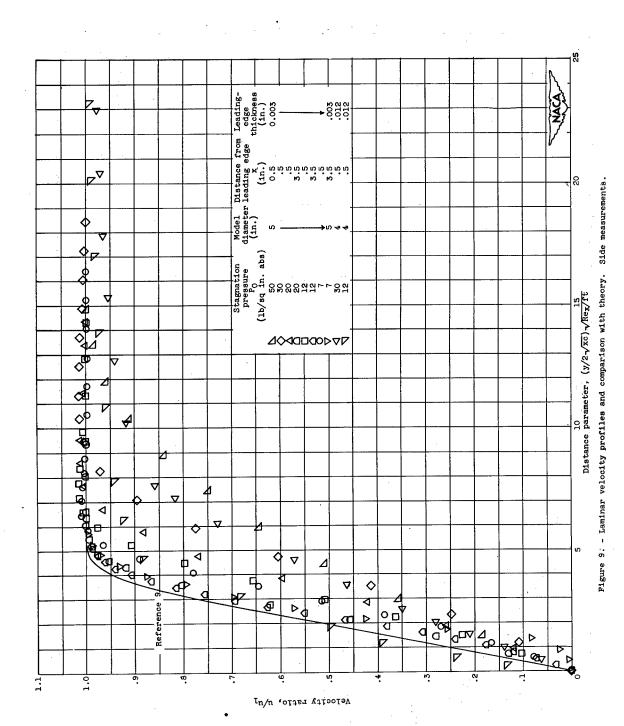
(b) Natural transition, stagnation pressure of 50 pounds per square inch absolute.

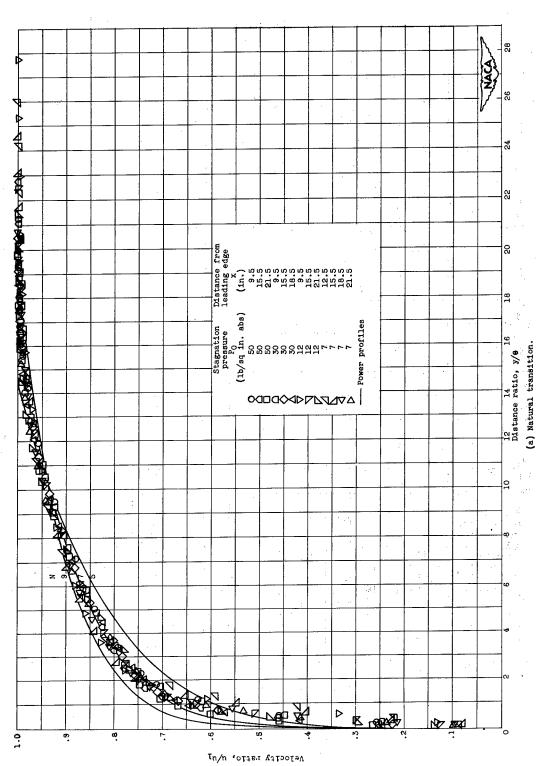
Figure 8. - Continued. Effect of leading-edge thickness on momentum thickness.



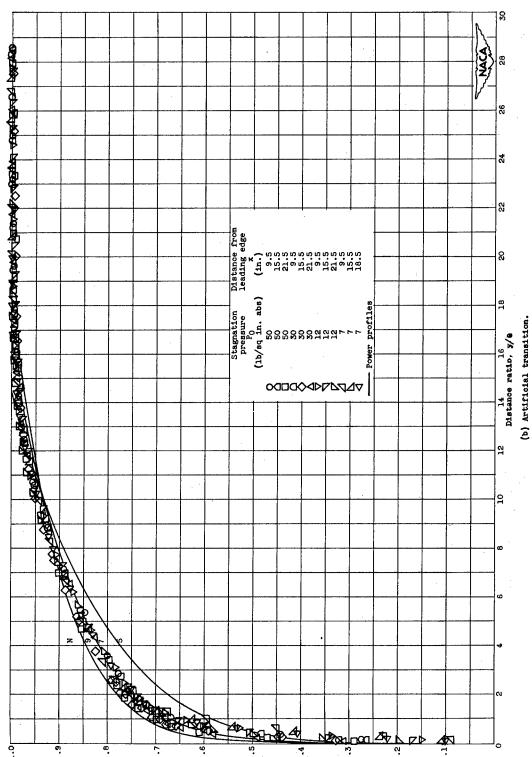
(c) Artificial transition, stagnation pressure of 12 pounds per square inch absolute.

Figure 8. - Concluded. Effect of leading-edge thickness on momentum thickness.





are 10. - Turbulent velocity profiles and comparison with power profiles for 5-inch model. Side measurem



Velocity ratto,  $u/u_{\perp}$ 

Figure 10. - Concluded. Turbulent velocity profiles and comparison with power profiles for 5-inch model. Side measurements.

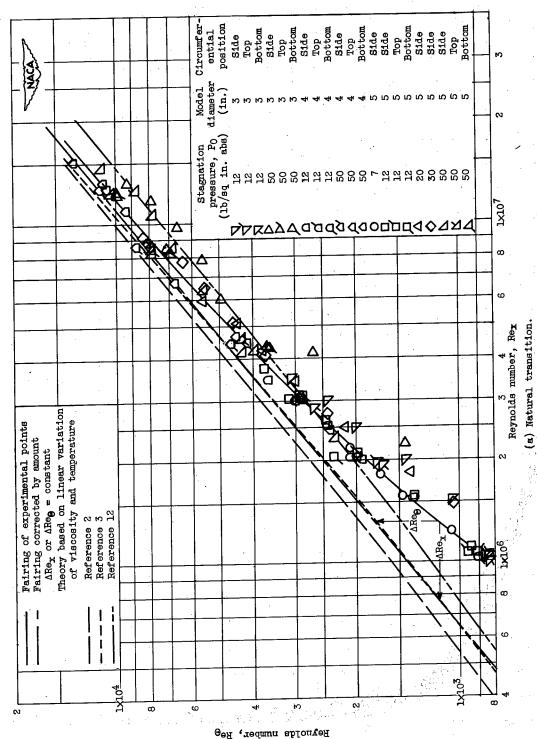


Figure 11. - Variation of Reg with Reg for 3-, 4-, and 5-inch cylinder models and comparison with theory.

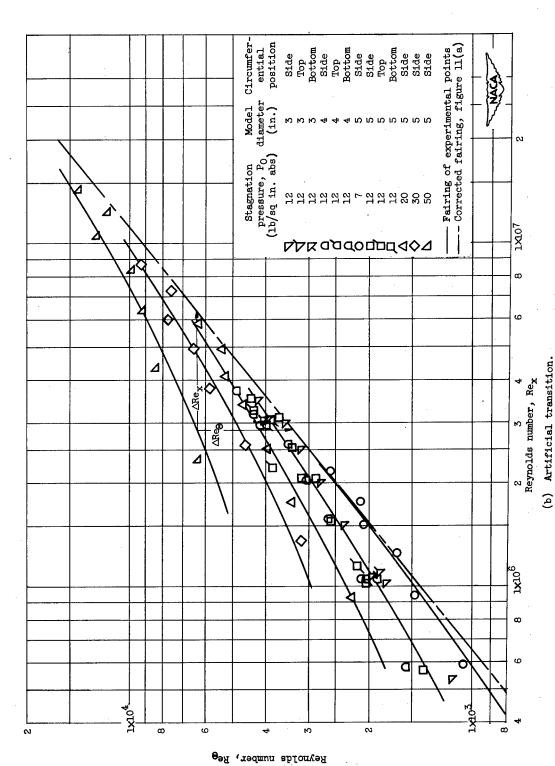
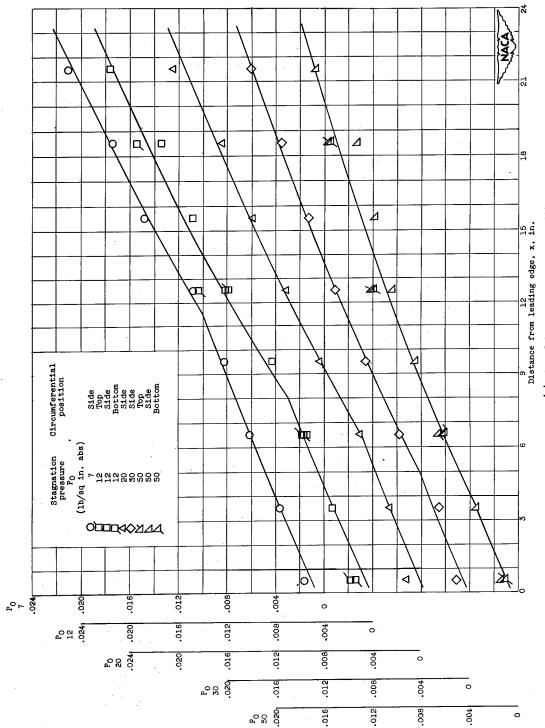


Figure 11. - Concluded. Variation of Reg with Rex for 3-, 4-, and 5-inch cylinder models and comparison with theory. Top, side, and bottom measurements.



(a) Along 5-inch model, natural transition.

Figure 12. - Momentum thickness distribution.

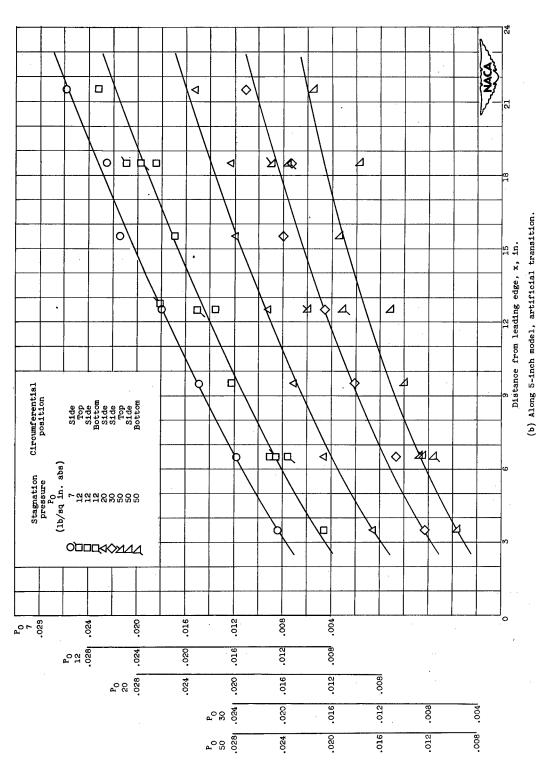
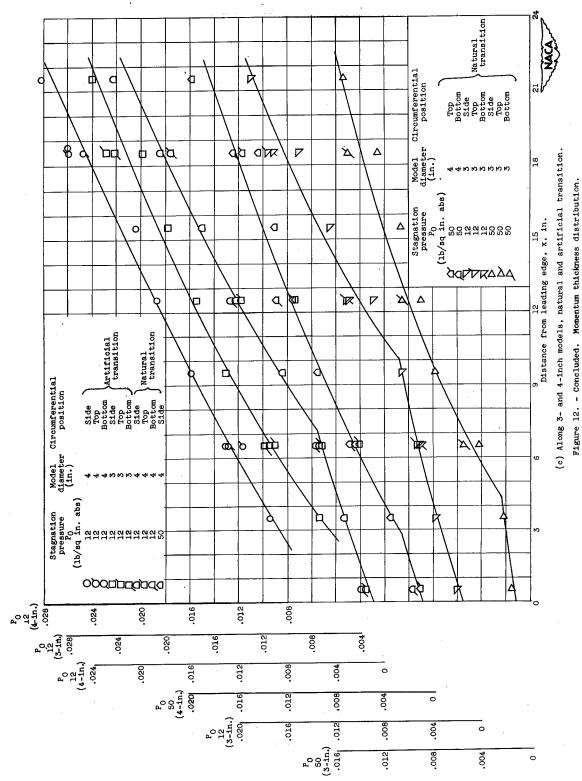


Figure 12. - Continued. Momentum thickness distribution.

Momentum thickness, 6, in.



Momentum thickness, 0, in.

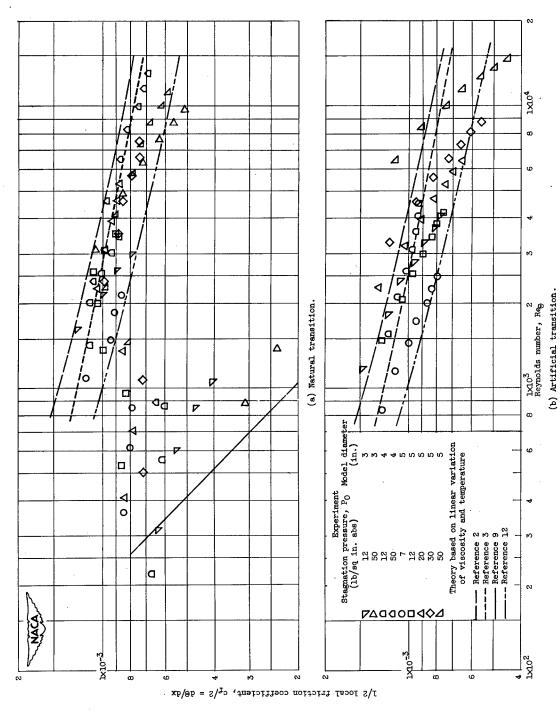
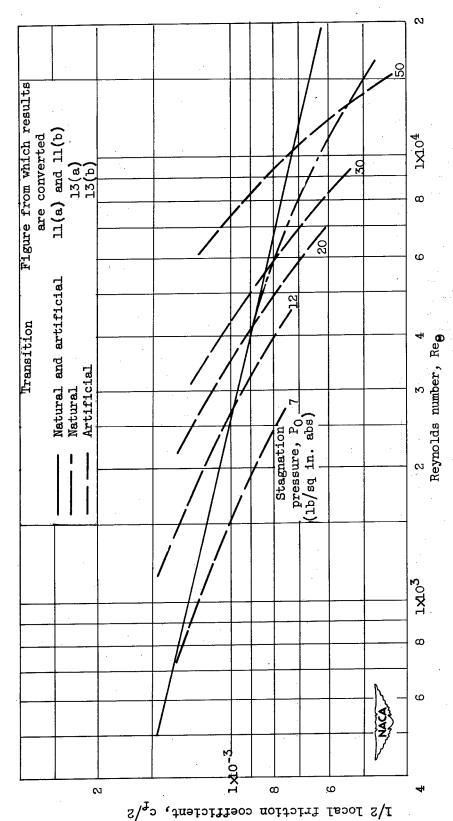


Figure 13. - Variation of local friction coefficient with Reg for 5-, 4-, and 5-inch models.



on 3-, 4-, and 5-inch models. Re Natural and artificial transition. Figure 14. - Summary of measured friction coefficients as function of

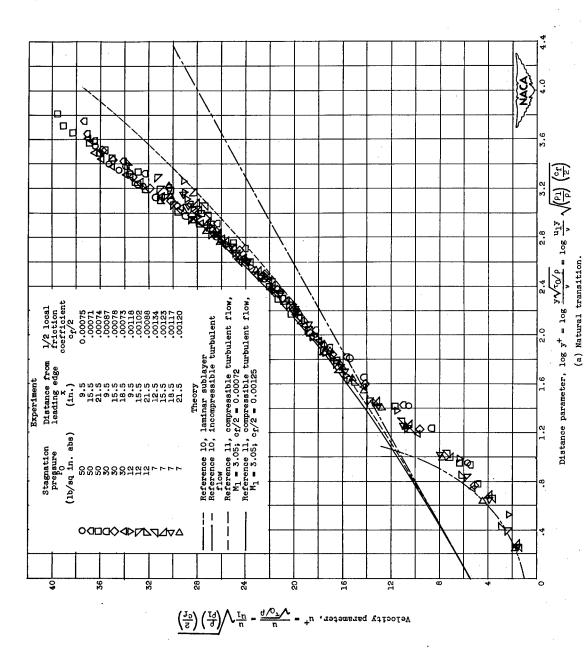


Figure 15. - Turbulent velocity profiles and comparison with theory. 5-inch model, side measurements.

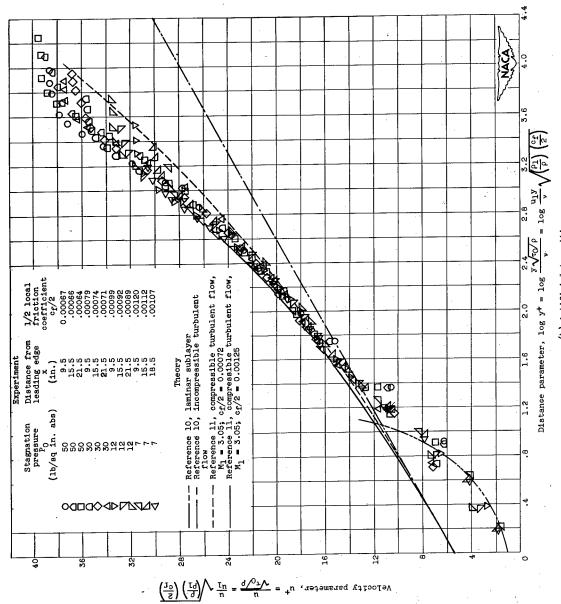
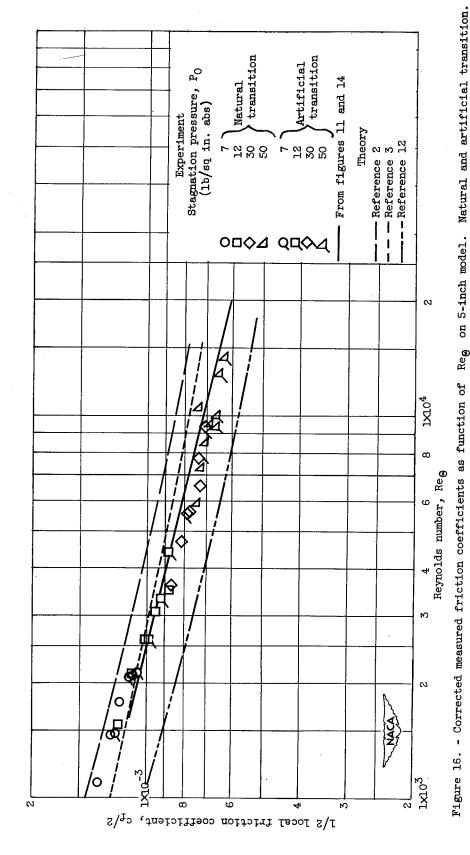


Figure 15. - Concluded. Turbulent velocity profiles and comparison with theory. 5-inch model, side measurements. (b) Artificial transition.

7Т



NACA-Langley - 7-17-52 - 1000

BOUNDARY-LAYER DEVELOPMENT AND SKIN Brinich and Nick S. Diaconis. July 1952. 49p. National Advisory Committee for Aeronautics. FRICTION AT MACH NUMBER 3.05. Paul F. diagrs., photos. (NACA TN 2742) NACA TN 2742

stream. Results were obtained for three model diameters and for natural and artificially induced turbulent Boundary-layer studies consisting of schlieren obsercylinder models with their axes alined parallel to the edge thickness and with reductions in tunnel pressure boundary-layer flows. Transition Reynolds numbers level. Turbulent temperature-recovery factors gen-Reynolds numbers. The results of this investigation vations and momentum surveys were made on hollow appeared to be consistent with the theoretical turbuerally decreased with increasing Reynolds number were found to decrease with decreases in leadingand were a maximum for the smallest transition

Copies obtainable from NACA, Washington

BOUNDARY-LAYER DEVELOPMENT AND SKIN

National Advisory Committee for Aeronautics. FRICTION AT MACH NUMBER 3.05. Paul F.

Brinich and Nick S. Diaconis. July 1952. 49p.

diagrs., photos. (NACA TN 2742)

(over)

(1.1.2.3)Flow, Supersonic ∺

Flow, Viscous (1.1.3) Brinich, Paul F., Jr. Diaconis, Nick S. 11日日

**NACA TN 2742** 

stream. Results were obtained for three model diameters and for natural and artificially induced turbulent Boundary-layer studies consisting of schlieren obseredge thickness and with reductions in tunnel pressure vations and momentum surveys were made on hollow cylinder models with their axes alined parallel to the boundary-layer flows. Transition Reynolds numbers level. Turbulent temperature-recovery factors gen-Reynolds numbers. The results of this investigation appeared to be consistent with the theoretical turbuerally decreased with increasing Reynolds number were found to decrease with decreases in leadingand were a maximum for the smallest transition

Copies obtainable from NACA, Washington

(over)

(1.1.2.3)Flow, Supersonic

Flow, Viscous (1.1.3) Brinich, Paul F., Jr. 21日日

Diaconis, Nick S. NACA TN 2742

BOUNDARY-LAYER DEVELOPMENT AND SKIN Brinich and Nick S. Diaconis. July 1952. 49p. National Advisory Committee for Aeronautics. FRICTION AT MACH NUMBER 3.05. Paul F. diagrs., photos. (NACA TN 2742)

(1.1.2.3)

Flow, Supersonic

Flow, Viscous (1.1.3)

Brinich, Paul F., Jr.

Diaconis, Nick S.

山田苗

NACA TN 2742

stream. Results were obtained for three model diameters and for natural and artificially induced turbulent Boundary-layer studies consisting of schlieren obsercylinder models with their axes alined parallel to the boundary-layer flows. Transition Reynolds numbers edge thickness and with reductions in tunnel pressure vations and momentum surveys were made on hollow level. Turbulent temperature-recovery factors gen-Reynolds numbers. The results of this investigation appeared to be consistent with the theoretical turbuerally decreased with increasing Reynolds number were found to decrease with decreases in leadingand were a maximum for the smallest transition

Copies obtainable from NACA, Washington

(over)

Flow, Supersonic

(1.1.2.3)

NACA TN 2742

BOUNDARY-LAYER DEVELOPMENT AND SKIN Brinich and Nick S. Diaconis. July 1952. 49p. National Advisory Committee for Aeronautics. FRICTION AT MACH NUMBER 3.05. Paul F. diagrs., photos. (NACA TN 2742)

eters and for natural and artificially induced turbulent stream. Results were obtained for three model diam-Boundary-layer studies consisting of schlieren obsercylinder models with their axes alined parallel to the boundary-layer flows. Transition Reynolds numbers edge thickness and with reductions in tunnel pressure vations and momentum surveys were made on hollow level. Turbulent temperature-recovery factors gen-Reynolds numbers. The results of this investigation appeared to be consistent with the theoretical turbuerally decreased with increasing Reynolds number were found to decrease with decreases in leadingand were a maximum for the smallest transition

Copies obtainable from NACA, Washington

(over)

Flow, Viscous (1.1.3) Brinich, Paul F., Jr. Diaconis, Nick S. NACA TN 2742 日日

## NACA TN 2742

lent friction formulas of Wilson and with the extended Frankl-Voishel analysis of Rubesin, Maydew, and Varga. Velocity profiles in the outer portion of the boundary layer could be approximated reasonably with a 1/7 power profile and were found to be approximately similar in this region. Velocity profiles given by the Kármán universal turbulent boundary-layer profile parameters were found to be similar in the laminar sublayer and in the turbulent region.

Copies obtainable from NACA, Washington

## NACA TN 2742

lent friction formulas of Wilson and with the extended Frankl-Voishel analysis of Rubesin, Maydew, and Varga. Velocity profiles in the outer portion of the boundary layer could be approximated reasonably with a 1/7 power profile and were found to be approximately similar in this region. Velocity profiles given by the Karmán universal turbulent boundary-layer profile parameters were found to be similar in the laminar sublayer and in the turbulent region.

SA S

Copies obtainable from NACA, Washington

## NACA TN 2742

lent friction formulas of Wilson and with the extended Frankl-Voishel analysis of Rubesin, Maydew, and Varga. Velocity profiles in the outer portion of the boundary layer could be approximated reasonably with a 1/7 power profile and were found to be approximately similar in this region. Velocity profiles given by the Karmán universal turbulent boundary-layer profile parameters were found to be similar in the laminar sublayer and in the turbulent region.

Copies obtainable from NACA, Washington

NACA TN 2742

lenf friction formulas of Wilson and with the extended Frankl-Voishel analysis of Rubesin, Maydew, and Varga. Velocity profiles in the outer portion of the boundary layer could be approximated reasonably with a 1/7 power profile and were found to be approximately similar in this region. Velocity profiles given by the Karmán universal turbulent boundary-layer profile parameters were found to be similar in the laminar sublayer and in the turbulent region.



NACA

Copies obtainable from NACA, Washington

NACA TN 2742 National Advisory Committee for Aeronautics. BOUNDARY-LAYER DEVELOPMENT AND SKIN FRICTION AT MACH NUMBER 3.05. Paul F. Brinich and Nick S. Diaconis. July 1952. 49p. diagrs., photos. (NACA TN 2742)	1. Flow, Supersonic (1.1.2.3) 2. Flow, Viscous (1.1.3) I. Brinich, Paul F., Jr. II. Diaconis, Nick S. III. NACA TN 2742	NACA TN 2742 National Advisory Committee for Aeronautics. BOUNDARY-LAYER DEVELOPMENT AND SKIN FRICTION AT MACH NUMBER 3.05. Paul F. Brinich and Nick S. Diaconis. July 1952. 49p. diagrs., photos. (NACA TN 2742)	1. Flow, Superson 1. Frinch, Viscous II. Erinich, Paul III. Diaconis, Nic. III. NACA TN 274
f schlieren of a made on he ed parallel three model three model induced tun tes in leadin n tunnel prevery factors ynolds num st transition his investige.		Boundary-layer studies consisting of schlieren observations and momentum surveys were made on hollow cylinder models with their axes alined parallel to the stream. Results were obtained for three model diameters and for natural and artificially induced turbulent boundary-layer flows. Transition Reynolds numbers were found to decrease with decreases in leadingedge thickness and with reductions in tunnel pressure level. Turbulent temperature-recovery factors generally decreased with increasing Reynolds number and were a maximum for the smallest transition Reynolds numbers. The results of this investigation appeared to be consistent with the theoretical turbu-	
Copies obtainable from NACA, Washington (Over)		Copies obtainable from NACA, Washington (OVer)	

